

Procedural Function-based Spatial Microstructures

<http://hm.softalliance.net/>

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Outline

- ◆ Heterogeneous objects modelling
- ◆ Natural and artificial microstructures
- ◆ Problems with surfaces & voxels
- ◆ Using real functions
- ◆ Regular and non-regular procedural microstructures
- ◆ Direct rendering and fabrication

Function Representation FRep

- ◆ Uniform representation of multidimensional point sets as

$$F(X) \geq 0$$

- ◆ Function $F(X)$ evaluation procedure traversing the construction tree structure
- ◆ Leaves: primitives
- ◆ Nodes: operations + relations

Constructive Hypervolume Model

Hypervolume is a multidimensional point set with multiple attributes

$$o = (F(X), S_1(X), \dots, S_k(X))$$

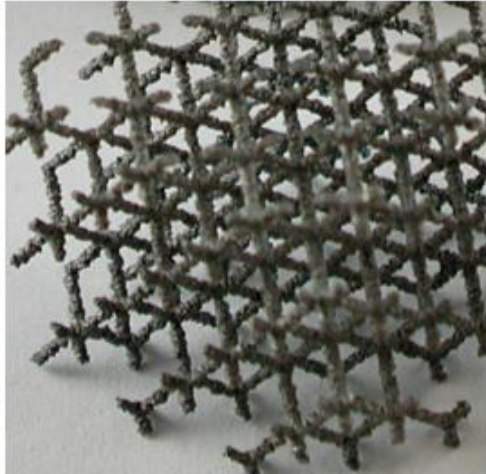
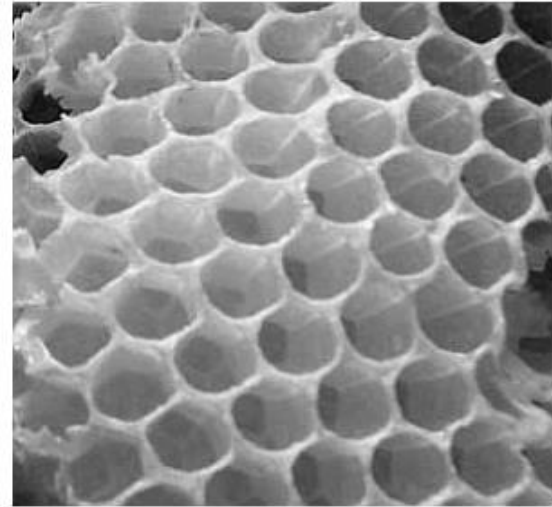
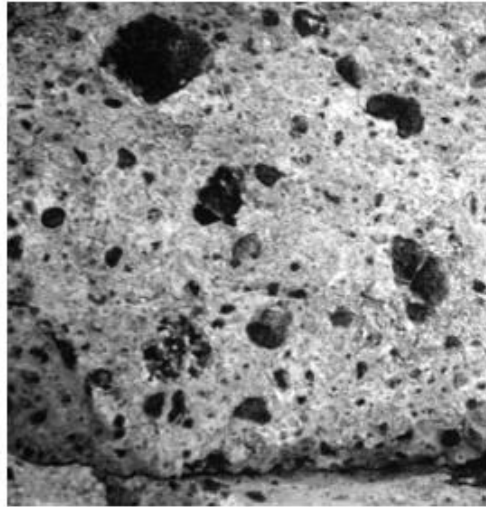
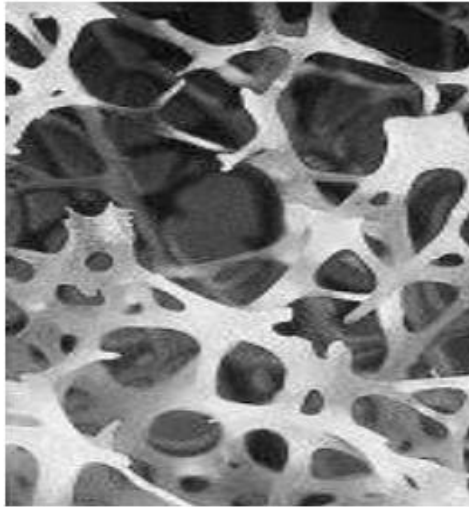
$F(X)$ – FRep of geometry

$S_i(X)$ – attributes based on FRep
space partitions

Heterogeneous objects

- ◆ Internal structure with non-uniform volumetric distribution of properties (density, color, transparency, etc.)
- ◆ Entities of different dimensionalities
- ◆ Gradually varying material distribution in CAD/CAM and fabrication
- ◆ Physical simulations, geological and medical modeling and rendering

Natural and artificial microstructures



Problems with surfaces & voxels

- ◆ **Size and processing time**
 - 100s Mb polygons, $>10^{10}$ voxels
- ◆ **Validity and precision**
 - cracks and approximations
- ◆ **Parameterization and operability**
 - blends, offsets, deformations
- ◆ **Manufacturability**
 - STL problems are amplified by the geometric complexity of microstructures

Procedural microstructures

Procedural generation of the defining function $F(X)$ value at the given point such that geometry of the entire microstructure is described as

$$F(X) \geq 0$$

Constructive model based on R-functions:

$$f_3 = f_1 \vee_{\alpha} f_2 \quad \text{for the union;}$$

$$f_3 = f_1 \wedge_{\alpha} f_2 \quad \text{for the intersection;}$$

Regular infinite lattices

Periodic infinite slabs

$$s_x(x, y, z) = \sin(q_x x + p_x) - l_x$$

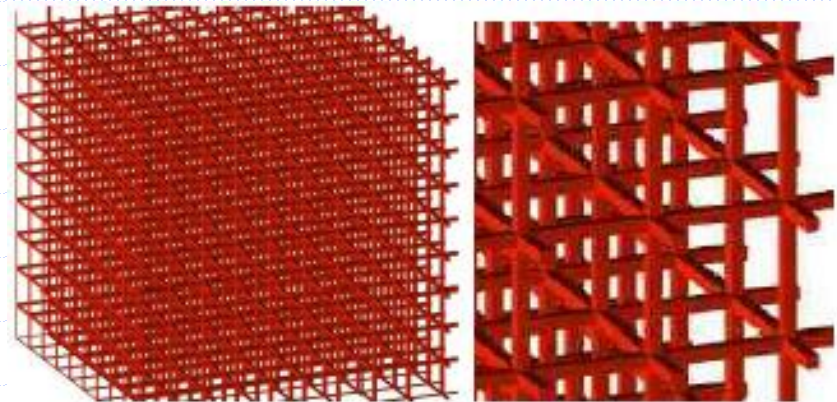
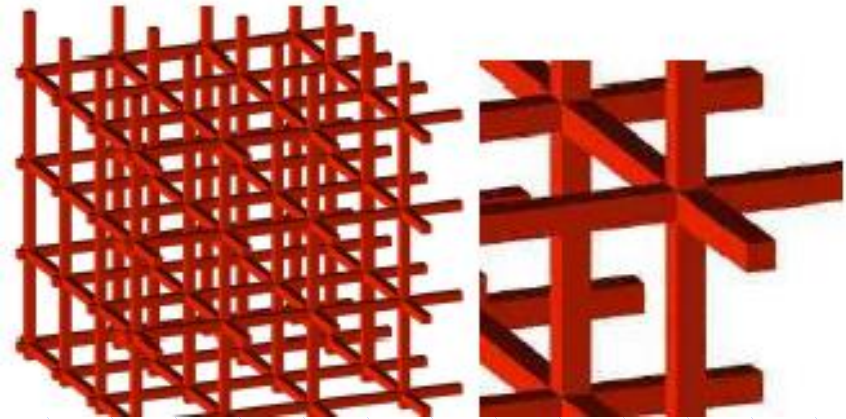
Rods: intersection of slabs

$$r_x(x, y, z) = s_y \wedge_\alpha s_z$$

Lattice: union of rods

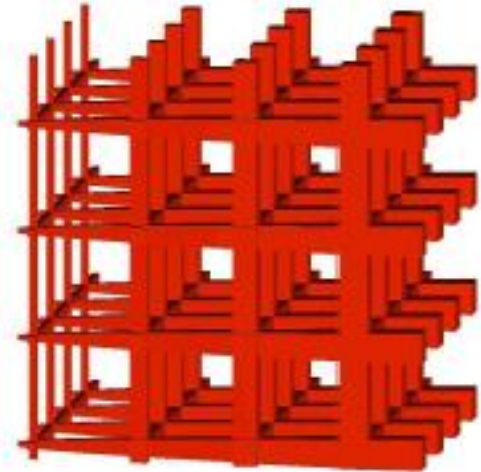
$$g(x, y, z) = r_x \vee_\alpha r_y \vee_\alpha r_z$$

$$g(x, y, z) = (s_y \wedge_\alpha s_z) \vee_\alpha (s_x \wedge_\alpha s_z) \vee_\alpha (s_x \wedge_\alpha s_y)$$

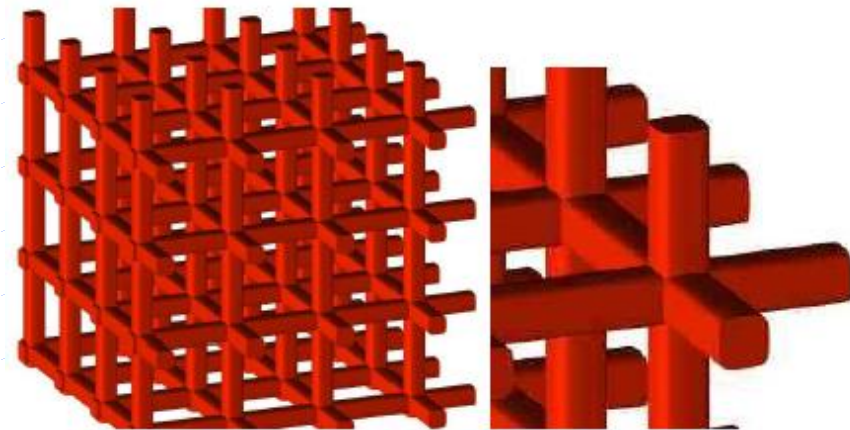


Variations of lattices

- ◆ Variable rod thickness

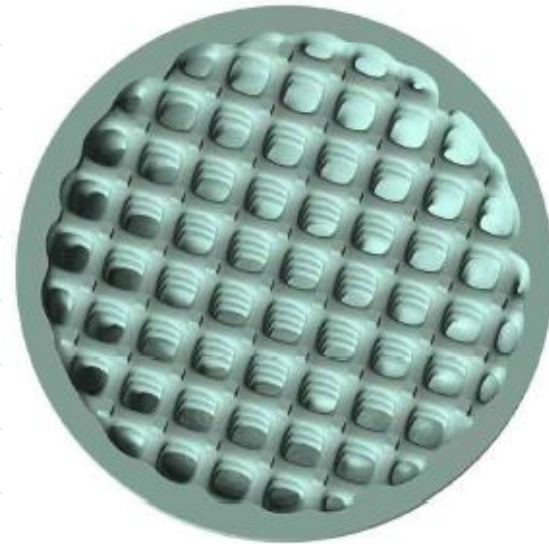
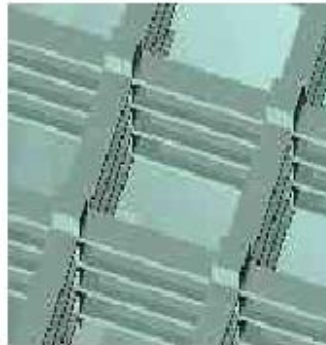


- ◆ Smoothed rods



$$f_1 \wedge_b f_2 = (f_1 \wedge_\alpha f_2) + \frac{a_0}{1 + \left(\frac{f_1}{a_1}\right)^2 + \left(\frac{f_2}{a_2}\right)^2}$$

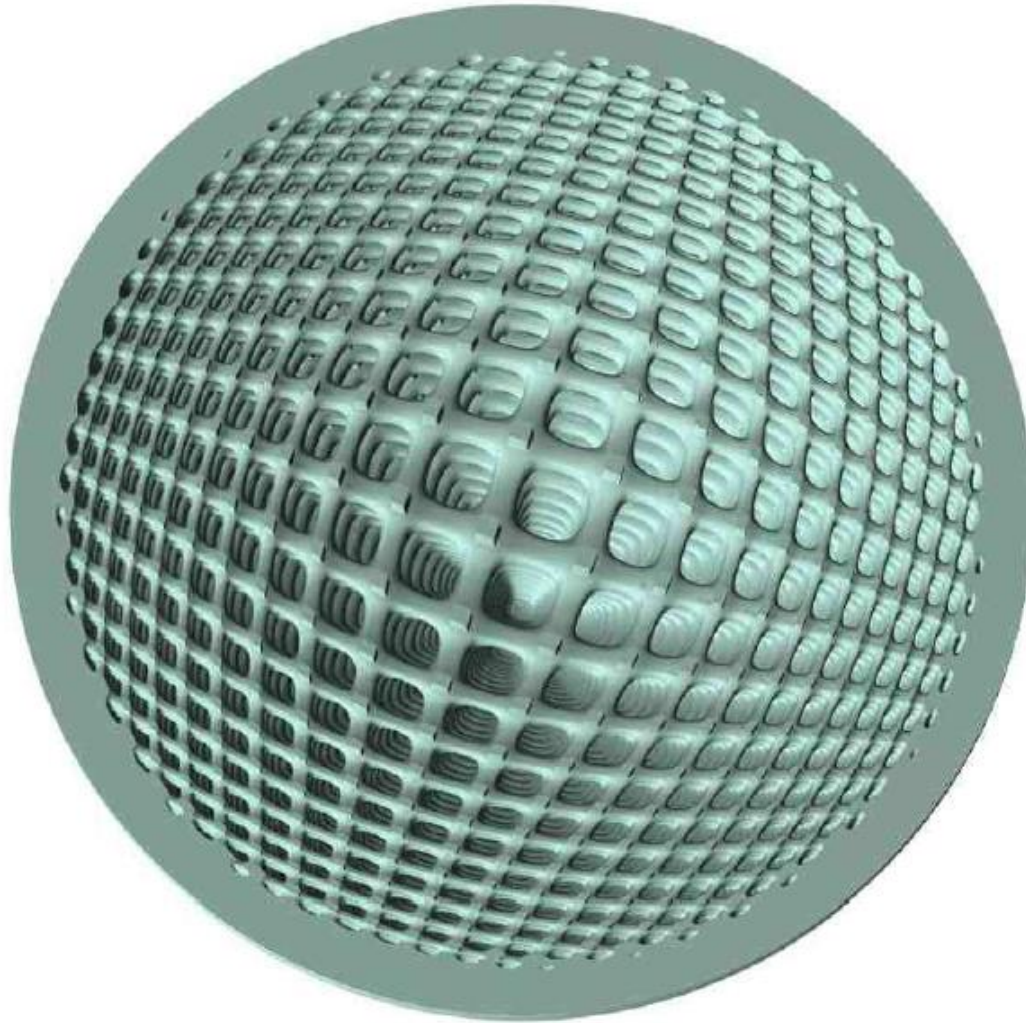
Combining with a shell



Truncation of a lattice by a solid and union with its shell

Blending union between rods and with a shell

Parameterization by distance

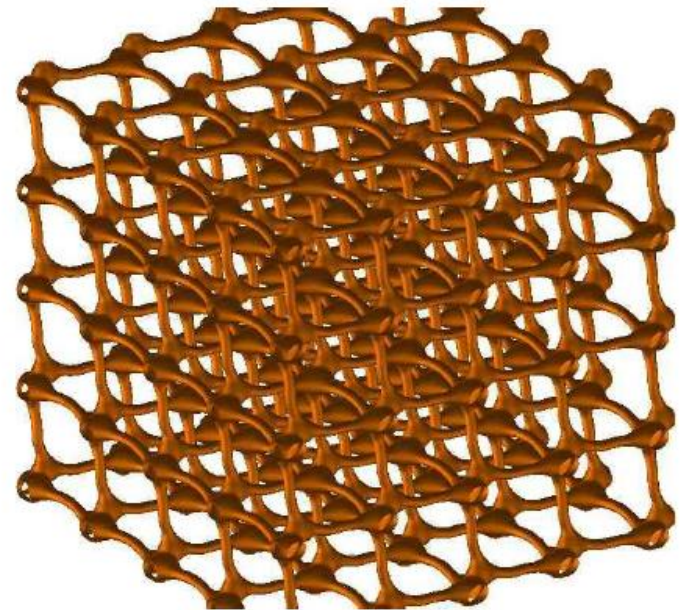
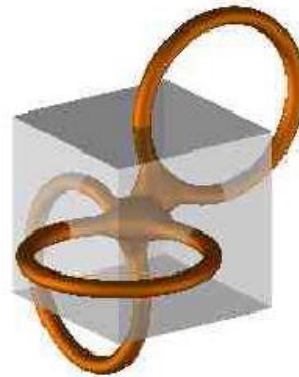


Lattice step decreases closer to the surface

Cellular microstructures

Replication of a unit cell with periodic space mapping:

$$x' = \text{perodic}(x)$$



Cellular microstructures

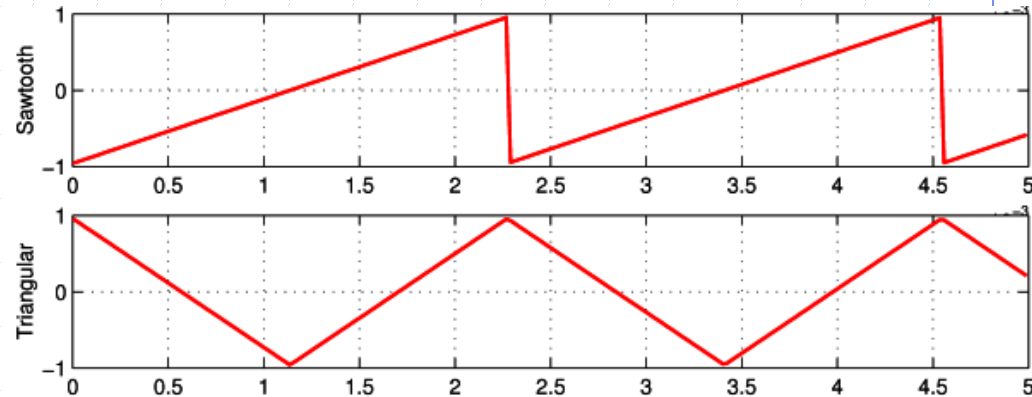
Non-symmetric cell -

sawtooth

Symmetric cell -

triangular

Sawtooth



Triangular

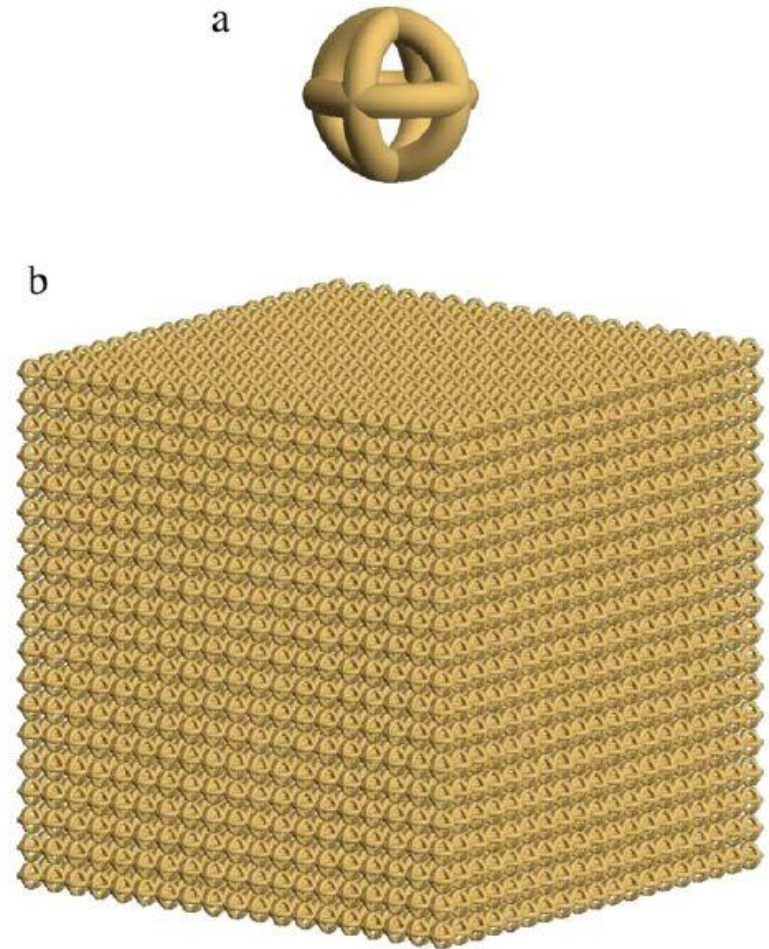
$$g(t) = \frac{1}{2} + \left(\frac{t}{a} - \text{floor} \left(\frac{t}{a} + \frac{1}{2} \right) \right)$$

$$g(t) = \frac{1}{2} + \frac{1}{\pi} \sin^{-1} \left[\sin \left(\pi \frac{t}{a} \right) \right]$$

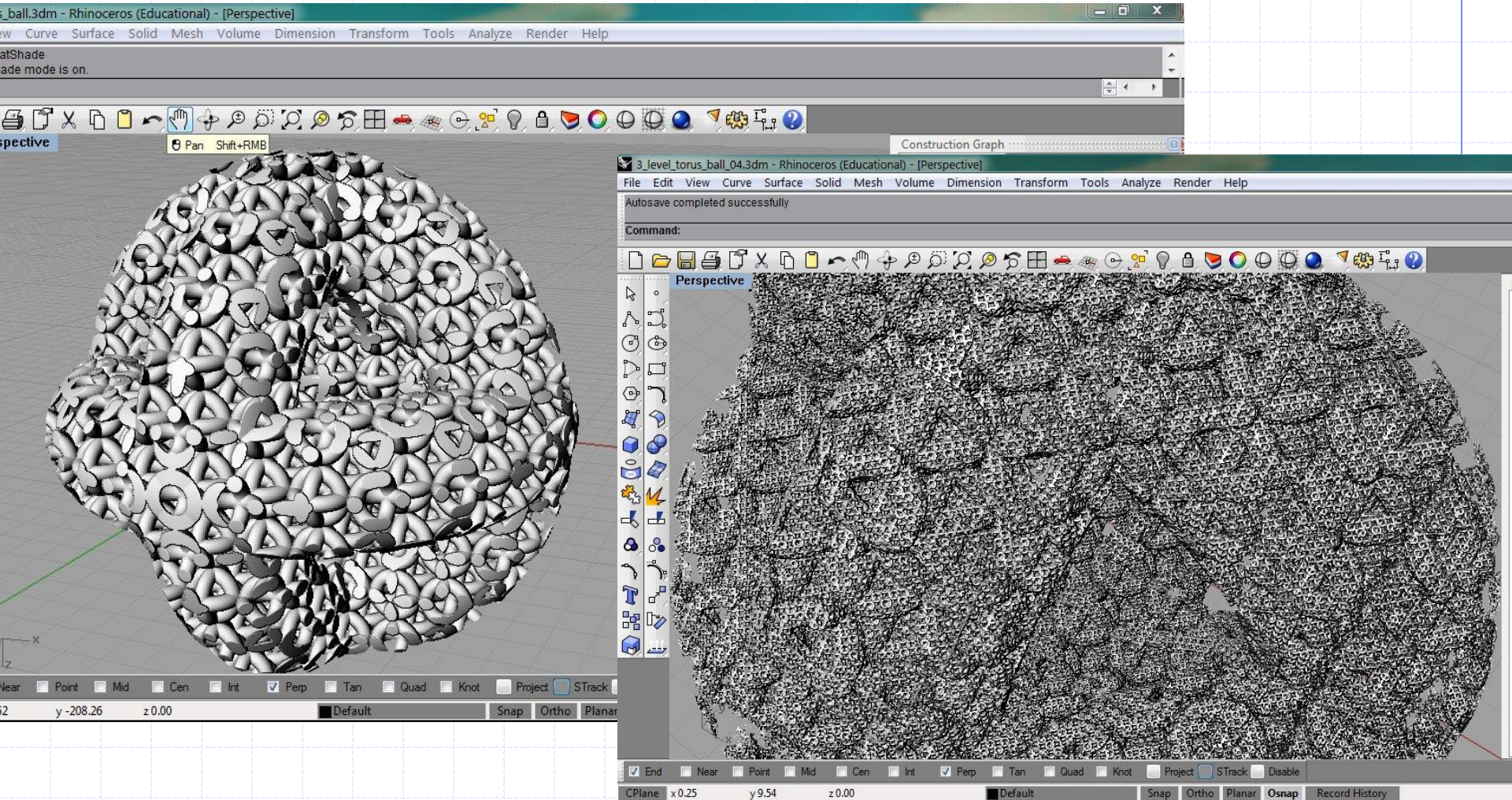
where a is a period of the function.

Cellular microstructures

Replication of a unit cell (a: union of three tori) with periodic space mapping (b: sawtooth or triangle)



Multi-scale nested FRep structures



3 levels of nested tori balls

Metamorphosis

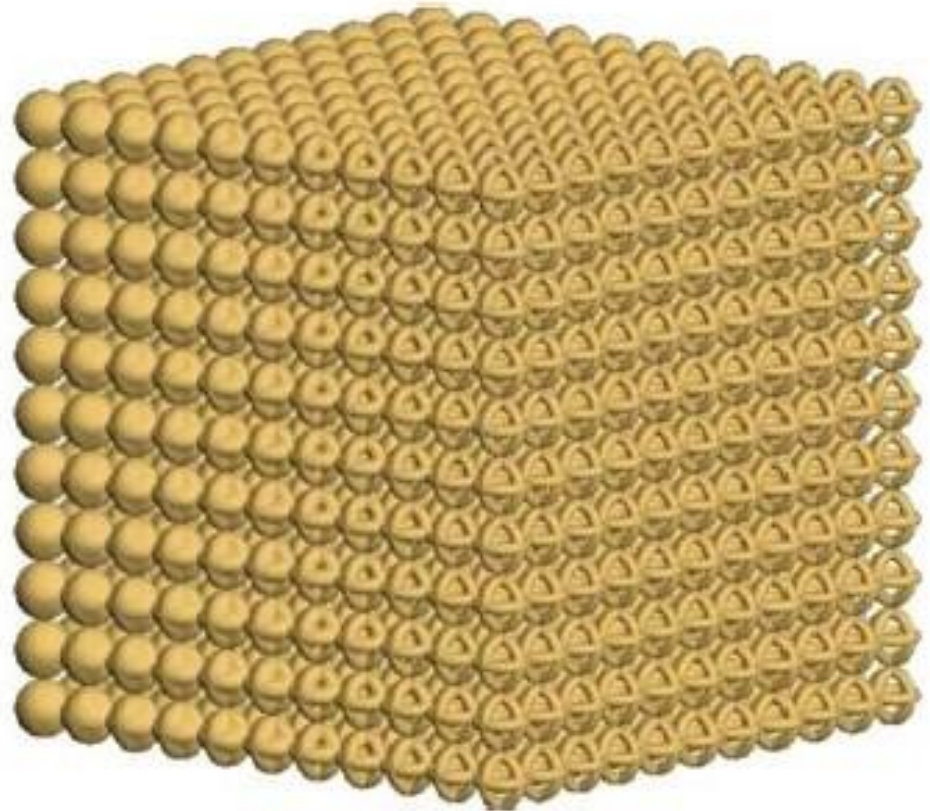
Spatial metamorphosis from a ball to a union of three tori:

$$f = f_1(1-t) + f_2t$$

$$t \in [0,1]$$

f₁ is a ball

f₂ is a union of three tori



Spatial interpolation

Cell metamorphosis:

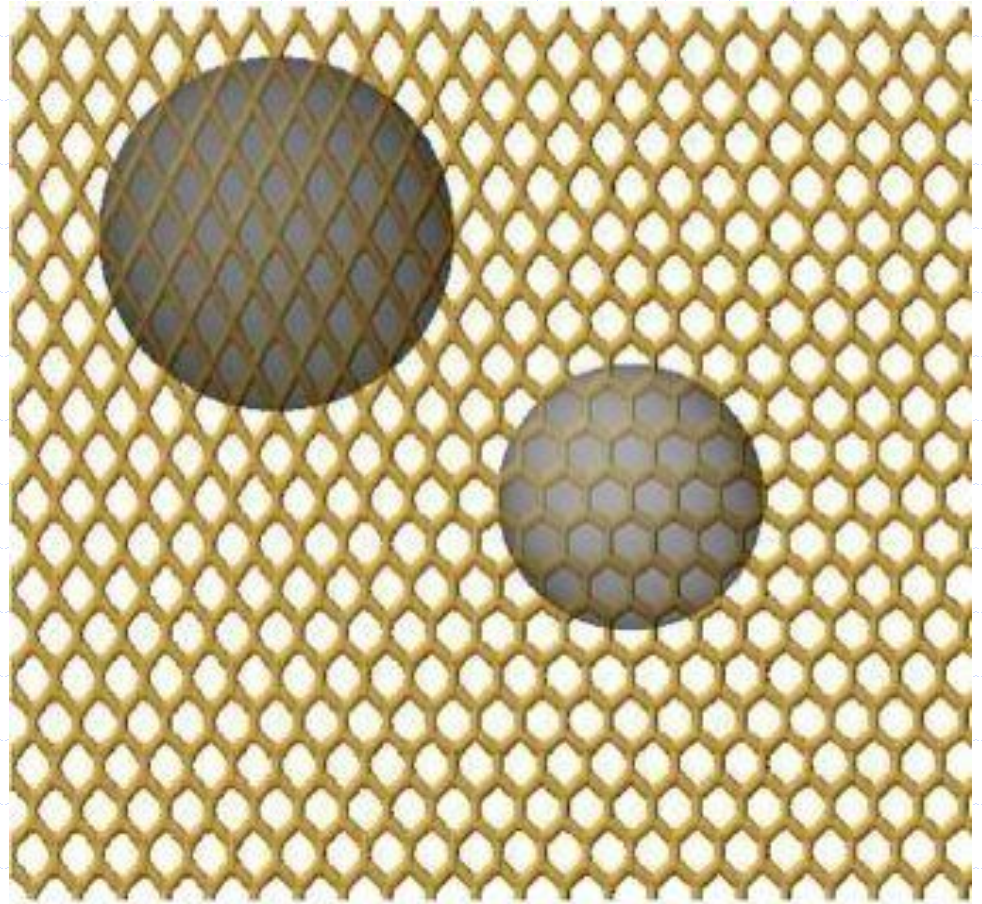
$$f = f_1(1-t) + f_2t$$

$$t \in [0,1]$$

f_1 is a rhomboid

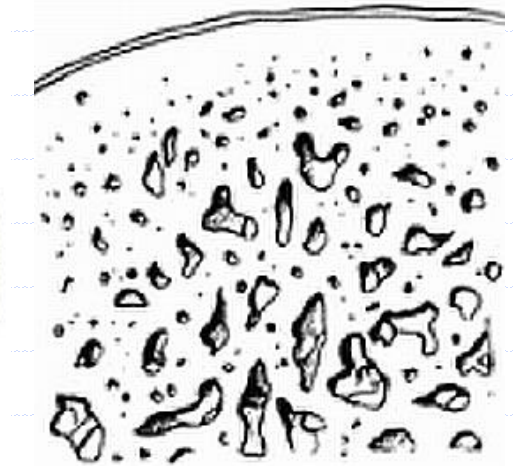
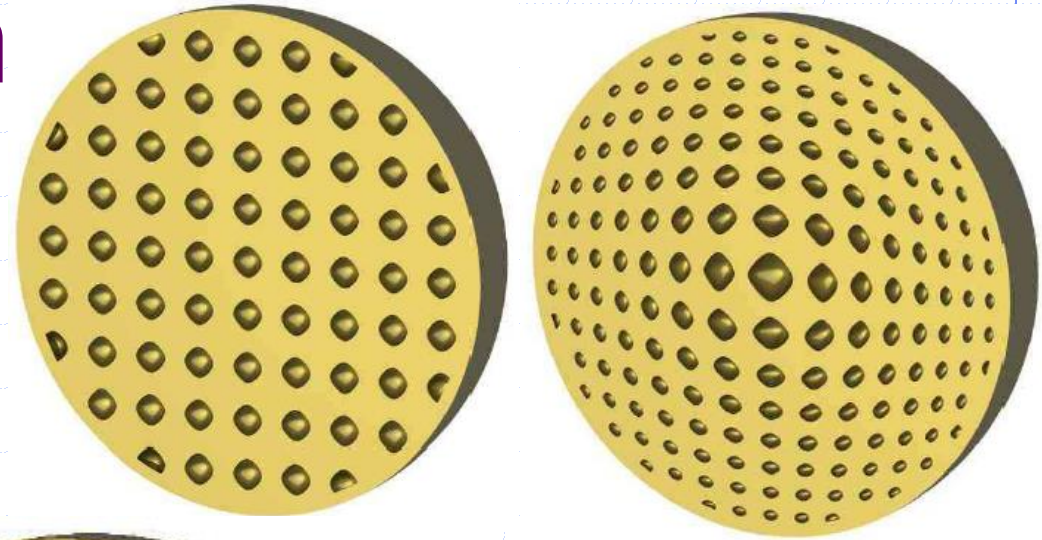
f_2 is a hexagonal lattice

or transfinite interpolation



Porous media

1. Basic pore replication
2. Distance dependency
3. Adding noise



Direct rendering

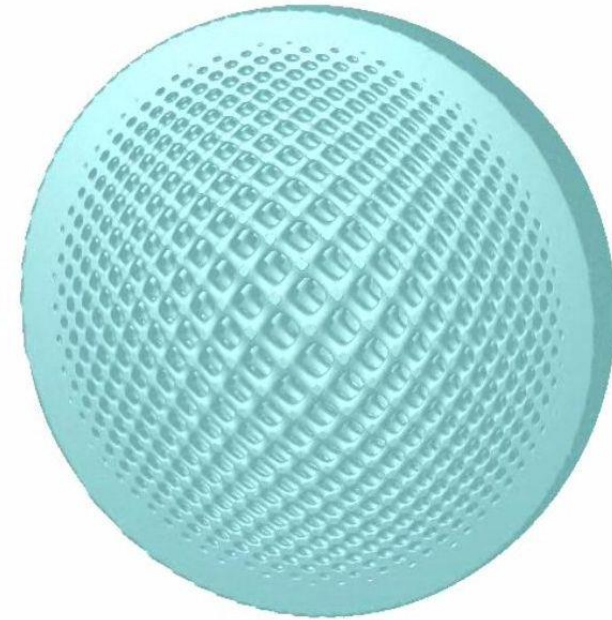
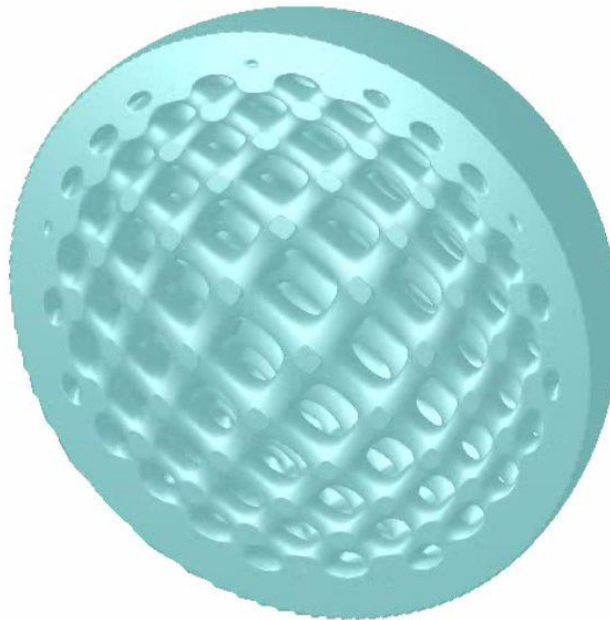
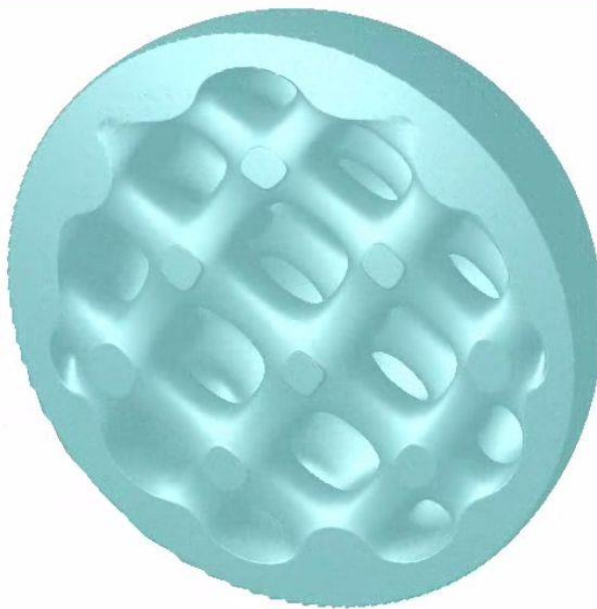
Real-time ray-tracing on GPU

independent of the microstructure density

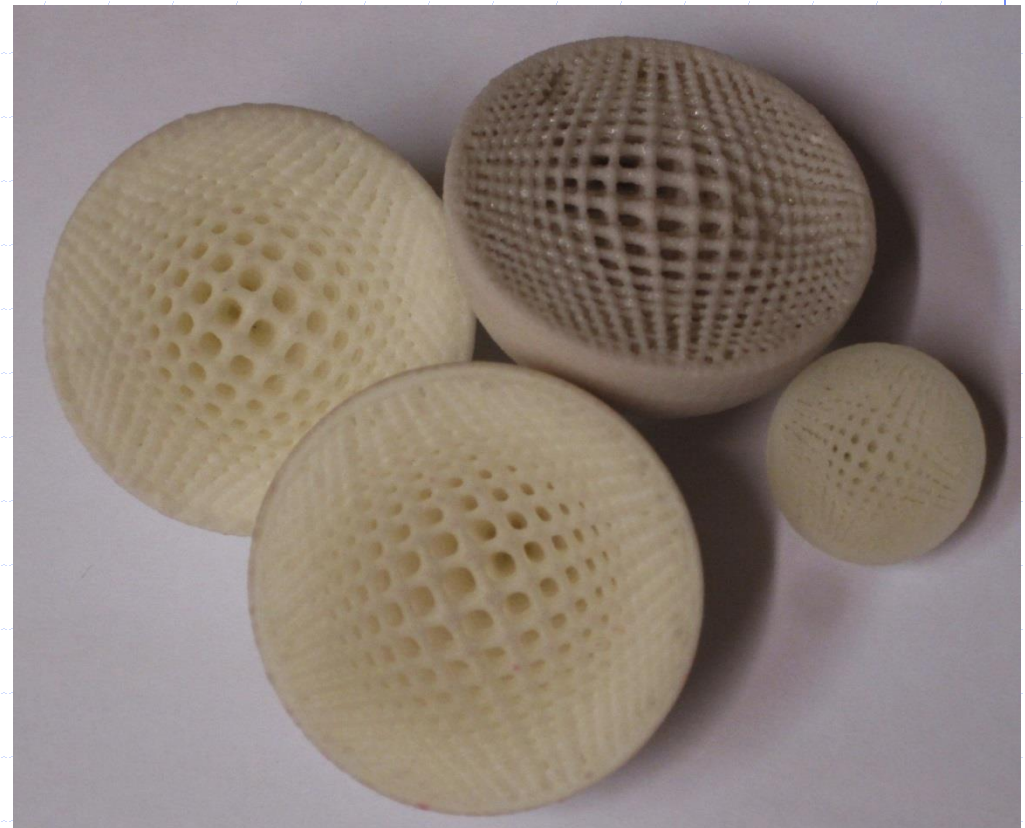


Direct rendering

with blending to the shell and between rods



Towards direct fabrication



- ◆ 3D Systems Sinterstation
- ◆ ZCorp 3D printer
- ◆ Stratasys Dimension

- ◆ STL problems
- ◆ Proprietary protocols

3D prints by the Centro de
Tecnologia da Informao,
CTI, Brasil

Applications

- ◆ Additive manufacturing / 3D printing
- ◆ Mechanical and bio-engineering
- ◆ Geological exploration
- ◆ Medicine
- ◆ Digital art and entertainment
- ◆ Creativity for disabled children - SHIVA project

Applications in 3D Printing



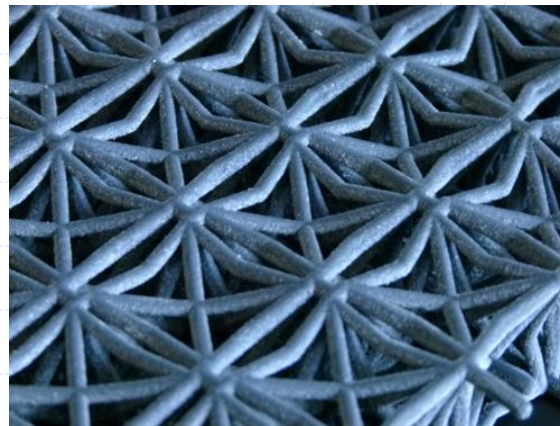
Chess pieces (resin & stereolithography)



Solver pendant (3D printed wax, casting)



Pavilion (concrete 3D print, D-shape)



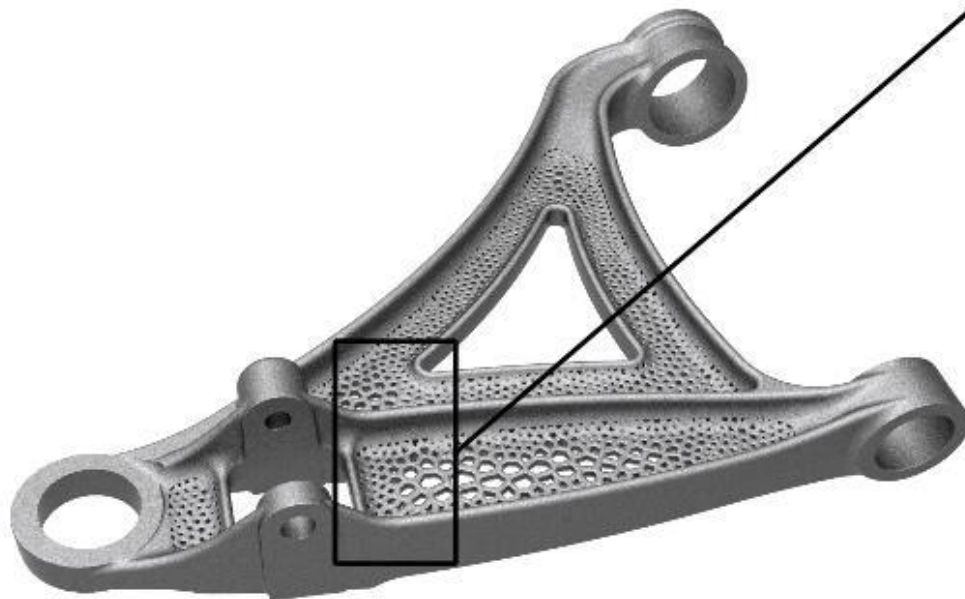
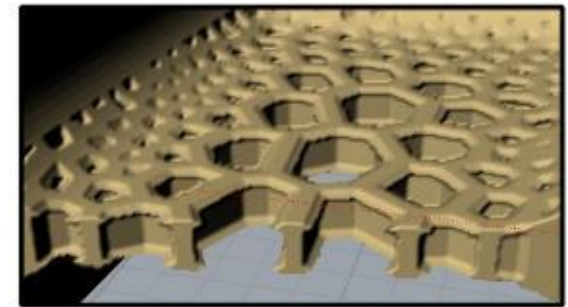
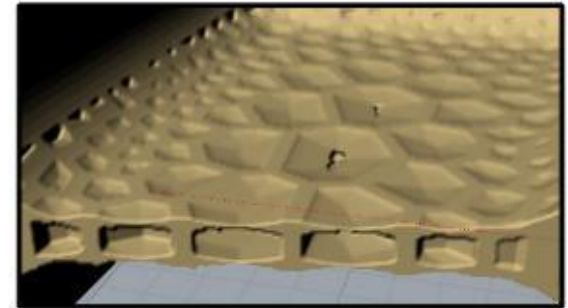
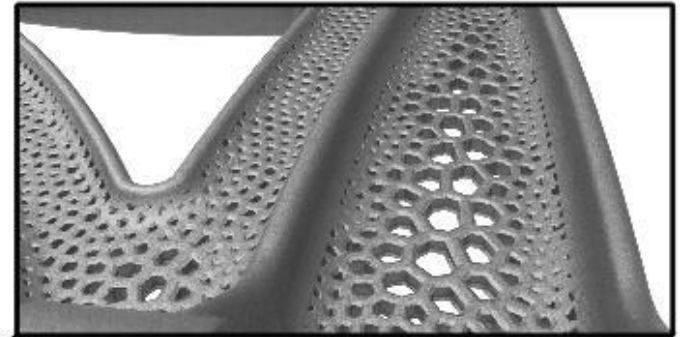
Construction pattern (plastic, ZCorp)



Bonbonniere (wood, milling machine)

Adaptive variable cellular and internal structures based on direct FEA and simulation feedback linked to dynamic generative parameters.

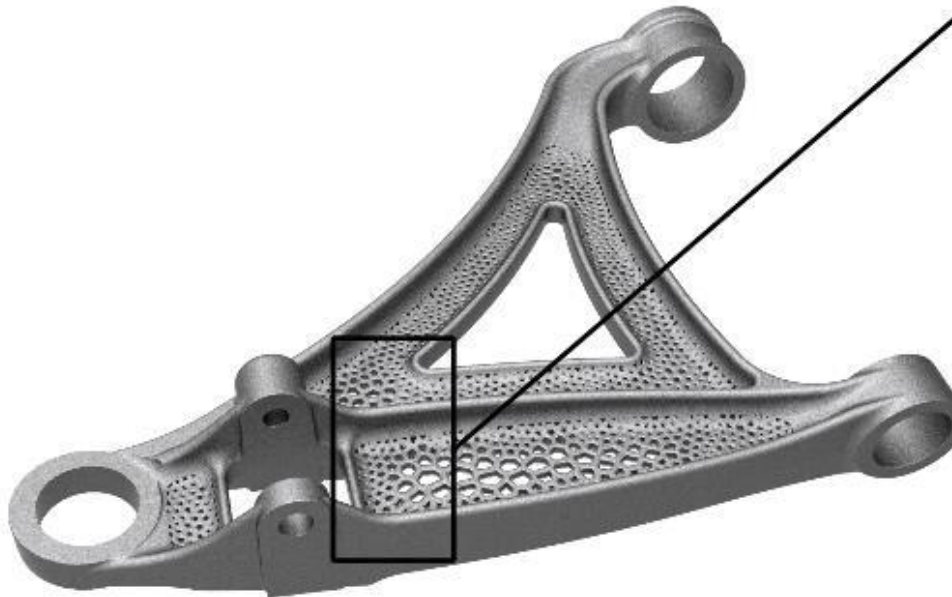
Ex 1: Simulation optimized & parameterized cellular structure with porous skin.



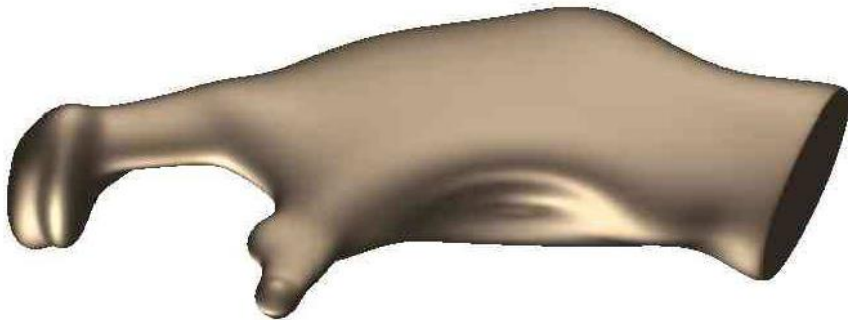
Next Steps – Advanced Designs w/ Automatic Closed Loop Simulation Feedback

Adaptive variable cellular and internal structures based on direct FEA and simulation feedback linked to dynamic generative parameters.

Ex 1: Simulation optimized & parameterized cellular structure with porous skin.



Lattice scaffold for a jaw bone



Initial jaw bone model



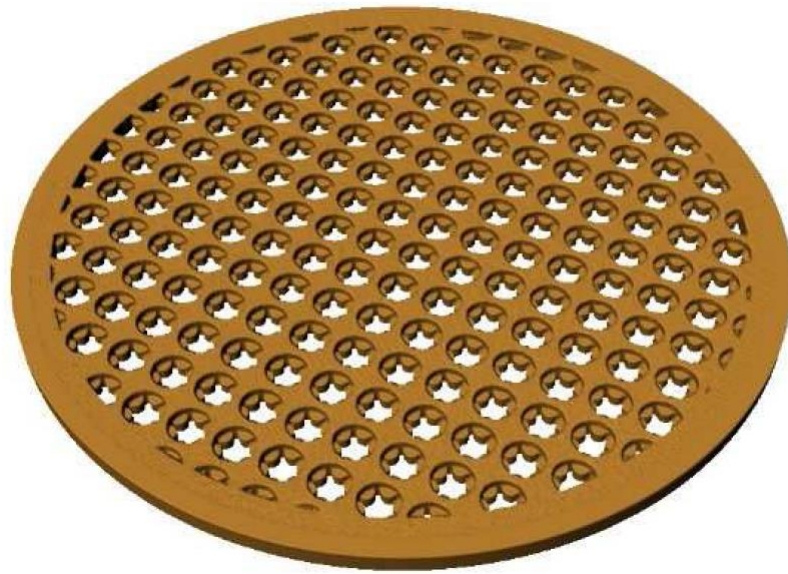
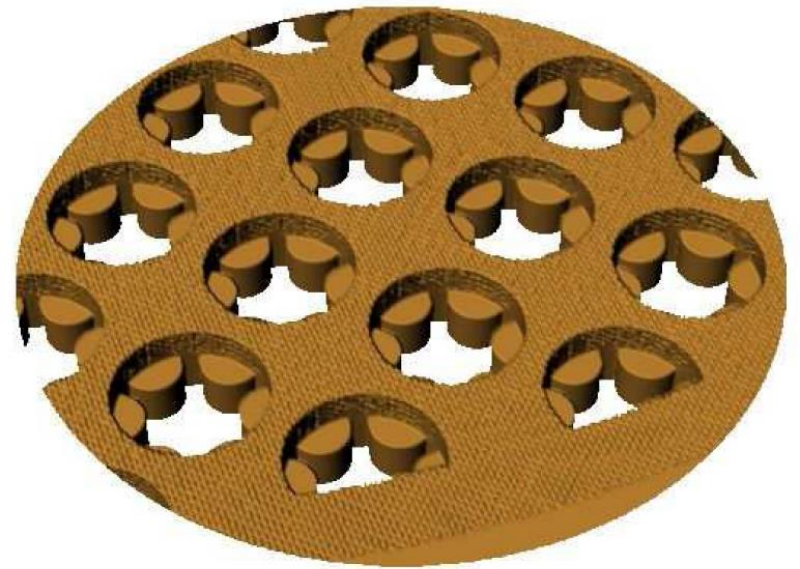
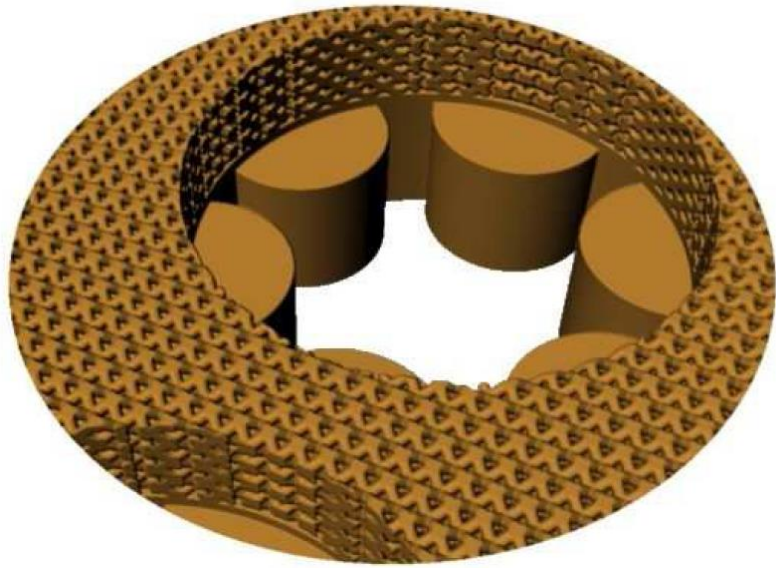
Union of lattice with bone shell



Lattice truncated by bone

Jaw bone model by
Denis Kravtsov

Filter design

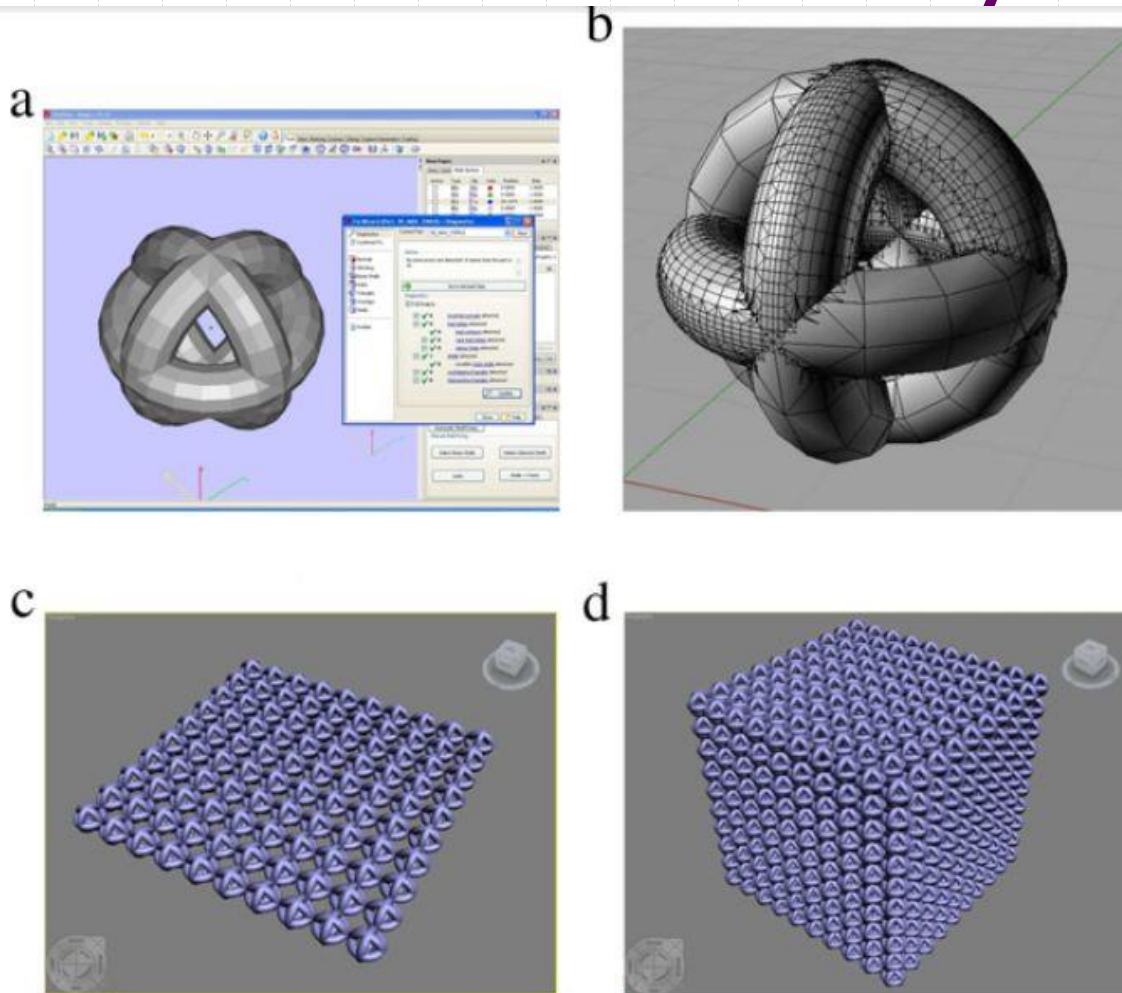


Surface design



Set-theoretic difference between the surface and the volume microstructure

Experiment with CAD systems



All CAD systems have failed the array of 100 tori balls

Conclusions

Polygon-free and voxel-free approach to

- ❖ Interactive modeling
- ❖ Real-time rendering
- ❖ Fabrication (ongoing)
- ❖ Fitting and analysis (future work)

Step towards procedural multiresolution modeling on micro- and nano-levels with infinite “zoom”.